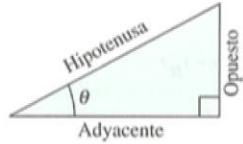


TRIGONOMETRÍA

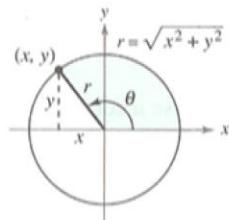
Definición de las seis funciones trigonométricas

Definiciones por triángulos rectángulos, donde $0 < \theta < \pi/2$.

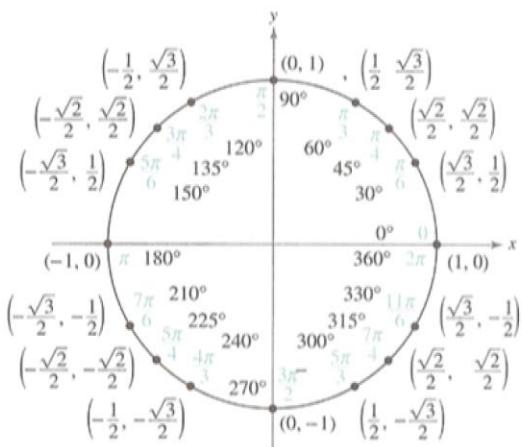


$$\begin{aligned}\operatorname{sen} \theta &= \frac{\text{op}}{\text{hip}} & \csc \theta &= \frac{\text{hip}}{\text{op}} \\ \cos \theta &= \frac{\text{ady}}{\text{hip}} & \sec \theta &= \frac{\text{hip}}{\text{ady}} \\ \tan \theta &= \frac{\text{op}}{\text{ady}} & \cot \theta &= \frac{\text{ady}}{\text{op}}\end{aligned}$$

Definiciones como funciones, donde θ es cualquier ángulo.



$$\begin{aligned}\operatorname{sen} \theta &= \frac{y}{r} & \csc \theta &= \frac{r}{y} \\ \cos \theta &= \frac{x}{r} & \sec \theta &= \frac{r}{x} \\ \tan \theta &= \frac{y}{x} & \cot \theta &= \frac{x}{y}\end{aligned}$$



Identidades recíprocas

$$\begin{aligned}\operatorname{sen} x &= \frac{1}{\csc x} & \sec x &= \frac{1}{\cos x} & \tan x &= \frac{1}{\cot x} \\ \csc x &= \frac{1}{\operatorname{sen} x} & \cos x &= \frac{1}{\sec x} & \cot x &= \frac{1}{\tan x}\end{aligned}$$

Identidades de tangente y cotangente

$$\tan x = \frac{\operatorname{sen} x}{\cos x} \quad \cot x = \frac{\cos x}{\operatorname{sen} x}$$

Identidades pitagóricas

$$\begin{aligned}\operatorname{sen}^2 x + \cos^2 x &= 1 \\ 1 + \tan^2 x &= \sec^2 x \quad 1 + \cot^2 x = \csc^2 x\end{aligned}$$

Identidades de cofunciones

$$\begin{aligned}\operatorname{sen}\left(\frac{\pi}{2} - x\right) &= \cos x & \cos\left(\frac{\pi}{2} - x\right) &= \operatorname{sen} x \\ \csc\left(\frac{\pi}{2} - x\right) &= \sec x & \tan\left(\frac{\pi}{2} - x\right) &= \cot x \\ \sec\left(\frac{\pi}{2} - x\right) &= \csc x & \cot\left(\frac{\pi}{2} - x\right) &= \tan x\end{aligned}$$

Fórmulas de reducción

$$\begin{aligned}\operatorname{sen}(-x) &= -\operatorname{sen} x & \cos(-x) &= \cos x \\ \csc(-x) &= -\csc x & \tan(-x) &= -\tan x \\ \sec(-x) &= \sec x & \cot(-x) &= -\cot x\end{aligned}$$

Fórmulas de suma y diferencia

$$\begin{aligned}\operatorname{sen}(u \pm v) &= \operatorname{sen} u \cos v \pm \cos u \operatorname{sen} v \\ \cos(u \pm v) &= \cos u \cos v \mp \operatorname{sen} u \operatorname{sen} v \\ \tan(u \pm v) &= \frac{\tan u \pm \tan v}{1 \mp \tan u \tan v}\end{aligned}$$

Fórmulas del ángulo doble

$$\begin{aligned}\operatorname{sen} 2u &= 2 \operatorname{sen} u \cos u \\ \cos 2u &= \cos^2 u - \operatorname{sen}^2 u = 2 \cos^2 u - 1 = 1 - 2 \operatorname{sen}^2 u \\ \tan 2u &= \frac{2 \tan u}{1 - \tan^2 u}\end{aligned}$$

Fórmulas de reducción de potencias

$$\begin{aligned}\operatorname{sen}^2 u &= \frac{1 - \cos 2u}{2} \\ \cos^2 u &= \frac{1 + \cos 2u}{2} \\ \tan^2 u &= \frac{1 - \cos 2u}{1 + \cos 2u}\end{aligned}$$

Fórmulas de suma-producto

$$\begin{aligned}\operatorname{sen} u + \operatorname{sen} v &= 2 \operatorname{sen}\left(\frac{u+v}{2}\right) \cos\left(\frac{u-v}{2}\right) \\ \operatorname{sen} u - \operatorname{sen} v &= 2 \cos\left(\frac{u+v}{2}\right) \operatorname{sen}\left(\frac{u-v}{2}\right) \\ \cos u + \cos v &= 2 \cos\left(\frac{u+v}{2}\right) \cos\left(\frac{u-v}{2}\right) \\ \cos u - \cos v &= -2 \operatorname{sen}\left(\frac{u+v}{2}\right) \operatorname{sen}\left(\frac{u-v}{2}\right)\end{aligned}$$

Fórmulas de producto-suma

$$\begin{aligned}\operatorname{sen} u \operatorname{sen} v &= \frac{1}{2}[\cos(u-v) - \cos(u+v)] \\ \cos u \cos v &= \frac{1}{2}[\cos(u-v) + \cos(u+v)] \\ \operatorname{sen} u \cos v &= \frac{1}{2}[\operatorname{sen}(u+v) + \operatorname{sen}(u-v)] \\ \cos u \operatorname{sen} v &= \frac{1}{2}[\operatorname{sen}(u+v) - \operatorname{sen}(u-v)]\end{aligned}$$